

[74r]

Ockham

Monday. 4<sup>th</sup> Jan y ['1841' added by later reader]

Dear M<sup>r</sup> De Morgan. We have had company ever since I last wrote to you, so I have been at a Stand-still, & only yesterday was able to read over with attention your replies. I am reluctant to trouble you again with remarks on the Series  $1 + \frac{x^2}{2} + \frac{x^4}{2.3.4} + \&c$ , for it seems as if I was determined to plague you about it. However I feel I must do so. Your added [74v] remarks of last time, about *B* &c, are quite clear in themselves, but I felt at once that they did not meet my difficulty which was that as long as  $\frac{5}{4}$  (which is greater than 1) is to be added to  $\frac{1}{2}\sqrt{1000,000} + \frac{1}{4}$ , it matters not whether for  $\sqrt{1000,000} + \frac{1}{4}$  we substitute the whole number next above it or "the intermediate fraction" alluded to by you in the line I have marked [mark a bit like her '√'], but we never can bring out  $n =$  to anything less than 502, whence  $n + 1$  the required term must [75r] be 503. This, after reading over & over, remains in my mind a most obstinate fact, and I believe I have found out the real source of the discrepancy between the result at the bottom of the first page & the top of the Second

one. I am presumptuous  
enough to think there is  
certainly an error in your  
writing out, in the line I  
have marked X, & it is one  
which is very likely to have  
occurred in writing ['it' crossed out] in  
a hurry. —

The  $(n + 1)^{\text{th}}$  term divided by  
the  $n^{\text{th}}$  is I believe not

[75v]  $\frac{Z}{(2n-2)(2n-3)}$ , but  $\frac{Z}{2n(2n-1)}$ ,

and I have re-written & now  
enclose the rest of the demonstration

(exactly like yours) with this  
correction. The result comes

out as I expected, owing to

$\frac{1}{4}$  taking the place of  $\frac{5}{4}$ ,

& everything appears to me

consistent. — the  $n^{\text{th}}$  term

divided by the  $(n - 1)^{\text{th}}$  term

would be, (as you have

written)  $\frac{Z}{(2n-2)(2n-3)}$ , & this

correction would do instead of

the others, & be perhaps ['a' inserted] more

simple mode of making it,

as your demonstration would

[76r] then remain correct, the  $n^{\text{th}}$

term being in that case the

required unknown one instead

of the  $(n + 1)^{\text{th}}$ . —

I am afraid all this is a

little complicated to explain

in letters, & perhaps I have

still not succeeded very

perfectly in doing so; but

I feel it now all very

clear in my own mind,

& am only anxious to receive

confirmation as to my being

right, both as satisfactory

to me in the present instance,

& as tending to give me

[76v] confidence in future in  
my own conclusions, or, (if  
I am in this case puzzle-  
-headed), a due diffidence  
of them. \_\_\_\_\_  
I therefore beg your indulgence  
for being so teasing. \_\_\_\_\_  
Believe me

Yours most truly  
A. A. Lovelace