

[176r] [diagram]  $(a - x)x \quad ax - x^2$

[further diagrams: one Pythagoras-related]

[176v] [Königsberg bridges diagrams, some with labels in Babbage's hand]

[Pythagoras-related diagrams]

[177r] [further Königsberg bridges diagrams and related jotting]

[in Babbage's hand] 1 No return

3

5

If there are an odd N° of Bridges      2 No ending except  
if you do not begin you must end      4                    in island  
in it

2 9 4

[written at 90°, spanning bottom of 176v and 177r] 7 5 3

6 1 8

[177v]

$$(a \pm b)^2 = a^2 + b^2 \pm 2ab$$

$$\sin \frac{1}{2}a = \sqrt{\frac{1}{2}R^2 - \frac{1}{2}R \cos a}$$

$$(a - b) \times (a + b)$$

for  $\cos a$  put  $\pm \sqrt{R^2 - \sin^2 a}$

$$= a^2 - b^2$$

$$\sin \frac{1}{2}a = \sqrt{\frac{1}{2}R^2 \mp \frac{1}{2}R \sqrt{R^2 - \sin^2 a}}$$

Let  $\sin \frac{1}{2}a = \frac{1}{2} \sqrt{R^2 + R \sin a} \mp \frac{1}{2} \sqrt{R^2 - R \sin a}$

$$\frac{1}{2}R^2 \mp \frac{1}{2}R \sqrt{R^2 - \sin^2 a} =$$

$$= \frac{1}{4}R^2 + \frac{1}{4}R \sin a \quad + \frac{1}{4}R^2 - \frac{1}{4}R \sin a \mp 2 \times \frac{1}{2} \times \frac{1}{2} \sqrt{R^2 + R \sin a} \times \sqrt{R^2 - R \sin a}$$

$$\mp \frac{1}{2}R \sqrt{R^2 - \sin^2 a} = \mp \frac{1}{2} \sqrt{R^2 + R \sin a} \times \sqrt{R^2 - R \sin a}$$

$$= \mp \frac{1}{2} \sqrt{R^4 - R^2 \sin^2 a} = \mp \frac{1}{2}R \sqrt{R^2 - \sin^2 a}$$

$$\mp \frac{1}{2}R \sqrt{R^2 - \sin^2 a} = \mp \frac{1}{2}R \sqrt{R^2 - \sin^2 a}$$